Multi-Physics Numerical Simulation of Thermoelectric Devices

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To optimize the performance of a thermoelectric device for a specific application, the device should be uniquely designed for the application. Achieving an optimum design requires accurate measurements and credible analysis to evaluate the performance of the device and its relationship with the device parameters. To do that, we designed, fabricated, and tested four devices based on Bi₂Te₃ and Sb₂Te₃. To evaluate the accuracy of our analysis, experimental measurements were compared with the numerical simulation performed using COMSOLTM. The two sets of results were found to be in full agreement. This is a proof of the accuracy of our experimental measurements and the credibility of our simulation. The study shows that testing or simulating the devices without heat sink will lead to skewed results. This is because the junction will not hold its temperatures value, but will, instead, automatically change its value to the direction of thermal equilibrium. The study shows also that there is no reciprocity between the input and the output characteristics of the devices. Therefore, a device optimized for cooling and heating may not be automatically optimized for energy harvesting. For heating and cooling, temperature sensitivity should be optimized; while for energy harvesting, voltage sensitivity should be optimized. Using heat sink, our devices achieved a voltage sensitivity of 187.77 μ V/K and a temperature sensitivity of 6.12 K/mV.

Keywords

Thermoelectric Devices, Multi-Leg Devices, Bi₂Te₃, Sb₂Te₃, COMSOL, Finite Element Simulation, Voltage Sensitivity, Temperature Sensitivity

1. Introduction

The theory of thermoelectric effects has been studied extensively by many groups. With the advancement in material engineering and device fabrication,

these devices have become more efficient and are being used in many applications. These devices are mainly divided into two major groups: The first group is based on Peltier effect [1] [2] [3] [4] and is used in cooling and refrigeration applications [5] [6]. These devices can be used in cooling or heating integrated circuits, biological and medical elements, medical sensors and devices, and other applications; The second group is based on Seebeck effect [2] [3] and is mainly used in energy harvesting [1] [7]-[12]. The energy harvesting devices can harvest wasted energy from factories, car exhausts, solar cells, power stations, and many other sources.

There are many types of materials that can be used to build thermoelectric devices and modules. These materials possess different ranges of Seebeck and Peltier effects [2]. Thermoelectric materials can be members of different groups. They can be from the Chalcogenides [13] [14] [15], the Skutterudites [4], the Half Heusler [16], the Clathrates [17] [18], and the TAGS [19] [20]. The most promising materials are the compounds based on Bismuth Telluride (Bi₂Te₃) and Antimony Telluride (Sb₃Te₃) [21] [22]. Bi₂Te₃ and Sb₃Te₃ can be grown using many growth techniques such as: electrochemical [23], electroplating [24], flash evaporation [25], thermal evaporation [26] and Pulsed Laser Deposition (PLD) [1] [21] [22] [27]. Each technique has its advantages and disadvantages as discussed in [2].

Thermoelectric devices have been modeled and simulated using several techniques. Spice program was used to simulate lumped and distributed parameter models [28] [29]. Bipolar and diode thermoelectric devices have been modeled analytically for cooling and heat generation applications [30] [31]. Thermoelectric devices have been modeled and simulated not only as individual devices but as a module for different applications [32] [33]. These devices have been also simulated using numerical techniques [33]-[38]. Modeling and simulation are used to design devices, simulate their operation, and evaluate their performance before the costly fabrication process.

In this paper, we report on the analysis and simulation of multi-leg thermoelectric devices using Bi_2Te_3 and Sb_3Te_3 . The study was conducted using the finite element (FE) multi-physics program, COMSOLTM [39]. The multi-leg devices under consideration were developed, fabricated, and tested by the authors [1]. In that study, electrical conductivity, Seebeck effect, and voltage sensitivity (S_v) were measured [1]. The main goal of this study is to verify the accuracy of the experimental measurements and understand the device behavior with and without employing heat sinks. COMSOL provided the accuracy of a numerical analysis and the flexibility of modeling to emulate a real case scenario.

2. Numerical Model

The differential equations used in our analysis are part of COMSOL Program [38]. In this work, we used the thermoelectric module, where both heat and Poisson's equations are used simultaneously to solve for the field variables tem-

perature, T, and voltage, V, [37] [39]. The partial differential equations used to obtain the device parameters are

$$\nabla \left(\left(\sigma \alpha^2 T + k \right) \right) \nabla T - \nabla \left(\sigma \alpha \nabla V \right) = \sigma \left(\left(\nabla \right)^2 + \alpha \nabla T \nabla V \right)$$
(1)

and

$$\nabla(\sigma\alpha\nabla T) + \nabla(\sigma\nabla V) = 0 \tag{2}$$

where σ is the electrical conductivity, α is Seebeck coefficient, and k is the thermal conductivity of the material. The simulation model, built in COMSOL, is explained in extensive details in references [37] [38].

The structure of each device was constructed in COMSOL. The fabricated device structure and the properties of every material were used to build the model. Si (100) substrates, with a diameter of 3-inch and a thickness of 380 μ m, were used. A3000 Å layer of SiO₂was placed as insulator on top of the substrates. The thermoelectric materials, Bi₂Te₃ andSb₂Te₃, and the copper electrodes were added according to the device design. The thicknesses of these layers is taken to be400nm, which is their actual thickness in the fabricated devices [1]. **Figure 1(a)** shows a photograph of the fabricated devices. **Figure 1(b)** shows the device geometry constructed using COMSOL. **Figure 2(a)** shows the masks used in the fabrication, which indicate the areas of the Bi₂Te₃, Sb₂Te₃, and cupper layers. The top green-red-green and the bottom green-blue-green structures are for the characterization of Bi₂Te₃ and Sb₂Te₃, respectively. The cross structures are the registration marks for mask alignment. It should be noted that the test devices and the registration marks have not been added to the COMSOL geometry.

3. Simulation and Analysis of the Devices Tested without Heat Sink

Four devices, Device-1, Device-2, Device-3, and Device-4, whose thermoelectric materials were deposited at 100°C, 200°C, 300°C and 400°C, respectively, are simulated. The geometries were constructed with the actual device dimensions. The values of σ and k, used in the simulation analysis, are the measured values

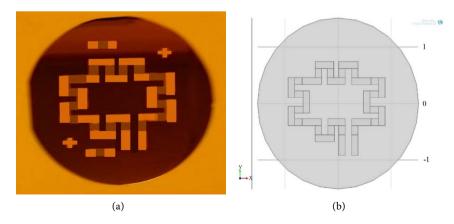


Figure 1. (a) A photograph of the device after fabrication [1]; and (b) The device geometry constructed using COMSOL.

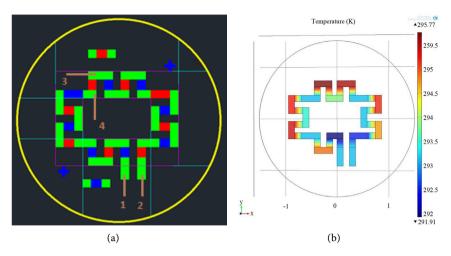


Figure 2. The 8-leg thermoelectric device: (a) The masks for the three layers: the red is for the Bi_2Te_3 , the blue is for Sb_2Te_3 , and the green is for the copper metal; (b) Temperature distribution obtained from applying a 0.3 mV across terminals 1 and 2.

shown in **Table 1**. The values of Seebeck coefficient were assumed to be -200×10^{-6} V/K for Bi₂Te₃, 200×10^{-6} V/K for Sb₂Te₃, and 6.5×10^{-6} V/K for copper [37]. For copper electrodes, an electric conductivity of 5.9×10^8 and a thermal conductivity of 350 were used [36] [37]. The thermal and electric conductivities for Bi₂Te₃ and Sb₂Te₃ are obtained from measurements and published literatures, and they are listed in **Table 1**. All other physical materials were obtained from COMSOL library.

The simulation shows that when a voltage was applied across terminals I and 2, a temperature difference was generated between terminals 3 and 4, as shown in **Figure 2(a)**. For device-1, when a voltage of 0.1 mV was applied, a temperature difference (ΔT) of 0.85 K was generated. And when the voltage increased to 0.2 mV and then to 0.3 mV, the temperature difference increased to 1.8 K and then to 2.67 K, respectively. **Figure 2(b)** shows one case of temperature simulation across the junctions, where an input voltage of 0.3 mV was applied. This voltage resulted in a temperature difference of 2.67 K. The figure shows also that the temperature difference is the same for each junction, while the electric potential decreases along the path from terminal 1 to terminal 2. This means that the junctions are thermally connected in parallel, but they are electrically connected in series. Simulations for other devices have produced similar results, but with different values. The values for the applied voltage and the corresponding temperature differences, for all devices, are shown in **Table 2**.

It has been observed from simulation that any increase in the applied voltage beyond certain values yielded no increase in the temperature difference. This appears to be a result of uncontrolled heat dissipation from the junctions, due to the absence of heat sink. The uncontrolled heat dissipation, made the device less sensitive to the applied voltage at higher values. This low sensitivity at higher voltages induced large errors, if S_v or S_T are obtained by curve fitting the entire V-T curve. Since the data at low voltages are more accurate, obtaining the

Devices	Thermal conductivity of Bi_2Te_3 (Wm ⁻¹ ·K ⁻¹)	Thermal conductivity of $Sb_2Te_3 (Wm^{-1} \cdot K^{-1})$	Resistivity of Bi ₂ Te ₃ ($\mu\Omega \cdot m$) (This work)	$\begin{array}{c} \text{Resistivity of Sb_2Te_3} \\ (\mu\Omega{\cdot}m) \\ (\text{This work}) \end{array}$
Device-1	1.75	1.63	40	24
Device-2	1.5	1.63	44	17.68
Device-3	0.9	1.63	68	16
Device-4	0.8	1.63	84	15

Table 1. Material properties used in the simulation [Ref. 24, 26, and 27 cited in [1]].

Table 2. Temperature difference between junctions 3 and 4, when voltages were applied at terminals 1 and 2 of the devices obtained from COMSOL simulation.

Voltage applied	ΔT (K)	$\Delta T (K)$	ΔT (K)	ΔT (K)
(mV)	Device-1	Device-2	Device-3	Device-4
0	0	0	0	0
0.1	0.85	0.78	0.85	0.85
0.2	1.8	1.8	1.48	1.8
0.3	2.67	2.67	1.68	2.58
0.4	-	3.15	2.91	3.44
0.5	-	-	4.16	4.16
0.6	-	-	5.28	5.28
-				

sensitivities values by obtaining the slope of the curve at lower temperatures would yield more accurate values.

Similar to Device-1, for Device-2, applying any voltage above 0.4 mV did not result in a significant change in the temperature. For Device-3 and Device-4, 0.6 mV was the voltage at which no significant difference in temperature was observed. The exact behavior of the four devices was observed experimentally too. The agreement between experimental measurements and simulation data for all devices proves the validity of this study, and it is a strong evidence of the accuracy of our findings and conclusions.

To characterize the device performance, we simulated the voltage sensitivity (S_v) and compared it to the corresponding experimental values. The sensitivity values for the simulation and experimental results are shown in **Table 3**. As shown in the table, the two sets of values are close to each other with about -7% to 20% difference. This deviation can be attributed to the use of constant values for Seebeck coefficient for all simulated devices; while in reality, Seebeck coefficient changes with the material growth conditions. The change of the Seebeck coefficient with growth temperature was automatically factored in the experimental measurements.

Temperature sensitivities ($S_T = 1/S_V$) for the devices were also calculated and their values are shown in **Table 3**, along with experimental results. As expected, the simulation values are in agreement with the experimental values, with deviation of -7% to 20%. Again this deviation can be attributed to the use of a

Device	Experimental values for S _V (μV/K)	Simulation values for S _v (µV/K)	Experimental values for S _T K/mV	Simulation values for $S_{\rm T}$
Device-1	93	112	10.75	8.93
Device-2	100	113	10	8.85
Device-3	146	135	6.85	7.41
Device-4	132	135	7.58	7.41

Table 3. Voltage Sensitivity ($S_V = \Delta V/\Delta T$) and Temperature Sensitivity ($S_T = \Delta T/\Delta V$) for experimental measurements [1] and COMSOL simulation (this work).

constant Seebeck coefficient for the thermoelectric materials, regardless of the growth temperature of the material. The decision to maximize S_V versus maximizing S_T depends on the application the device will be used for. For example, for power harvesting applications, S_V should be maximized. On the other hand, for cooling/heating applications, S_T should be optimized. In these cases, the device parameters, the geometries, and the fabrication process should be optimized for the intended goal.

4. Analysis of the Devices with Heat Sink

To obtain a better understanding of the performance, the devices were simulated again, but using a heat sink. In this case, the inner junctions, indicated as (I) in Figure 3, were kept at 293 K, while the temperature of the outer junctions, indicated as (O), varied from 293 K to 323 K. The electromotive force (emf), or the potential, created across terminals 1 and 2 was obtained. In addition, the heat flux across the junctions in both the x and y directions were simulated. The heat flux was simulated in order to understand the direction of heat flow, and to know whether heat is confined to the junctions or dissipate to the surroundings. As can be seen from Table 4, the temperature of the outer junctions increased from T = 293 K to T = 323 K in a 6-degree increment. This resulted in temperature difference from 0 to 30 K. The temperature difference, in turn, generated a voltage difference across terminals 1 and 2, as shown in Figure 2. Table 4 shows the voltage across the two terminals, the temperature of the hot junctions, and the temperature difference between the hot and the cold junctions. To obtain the voltage sensitivities, the voltage generated across terminals 1 and 2 are plotted against the temperature, as shown in Figure 4.

As can be seen from **Figure 4**, the relationship between the applied voltage and the temperature is slightly nonlinear, bending to the right. However, the relationship can still be approximated as a straight line. The slopes of these lines represent the voltage sensitivities (S_v) for the devices. **Table 5** shows the device voltage sensitivities for Device-1, Device-2, Device-3, and Device-4 to be 175.56, 163.33, 177.77, and 187.77 μ V/K, respectively. The Table shows also that the temperature sensitivities are 5.7, 6.12, 5.62, and 5.33 K/mV, respectively. Since S_T is the reciprocal of S_v , it is expected that devices with high voltage sensitivities will have low temperature sensitivities. The value of the sensitivity that matters

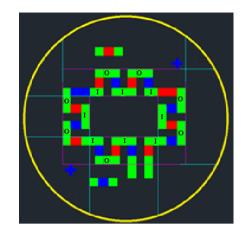


Figure 3. Thermoelectric device structure indicating the position of the inner and the outer parts of junctions.

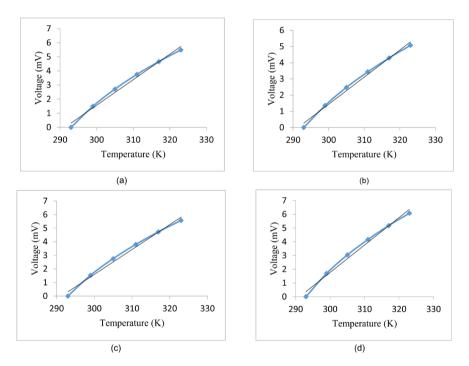


Figure 4. Voltage generated across terminals 1 and 2 when temperature difference is maintained across the device junctions: (a) Device-1; (b) Device-2; (c) Device-3; and (d) Devices-4, with the temperature of the inner junctions is fixed at 293 K.

Table 4. Voltage generated across terminals 1 and 2 as a result of temperatures difference across the junctions. The temperature of the inner junctions is kept at 293 K.

Temperature of outer junction (K)	-	Voltage (mV) Device @100°C	0 , ,	0, ,	0 , ,
293	0	0	0	0	0
299	6	1.50	1.36	1.53	1.70
305	12	2.71	2.48	2.75	3.04
311	18	3.75	3.44	3.80	4.17
317	24	4.66	4.30	4.73	5.18
323	30	5.49	5.08	5.57	6.08

depends on the application the device is intended for. For devices designed for cooling applications, the values of S_T should be maximized. But for devices intended for energy harvesting, the value of S_v should be the one to be maximized.

COMSOL simulation of Device-3 with outer junction temperature of 317 K is shown in **Figure 5**, as an example of the simulations results for this case. Similar results were obtained for all four devices, as explained before. **Figure 5(a)** shows the Temperature distribution, **Figure 5(b)** shows the Voltage distribution, **Figure 5(c)** shows the Heat Flux in the *x*-direction, and **Figure 5(d)** shows the Heat

Table 5. COMSOL simulation of Voltage Sensitivity ($S_V = \Delta V / \Delta T$) and Temperature Sensitivity ($S_T = \Delta T / \Delta V$) for devices with heat sink.

Device	$S_{\rm V}$ (µV/K) with heat sink	S_T (K/mV) with heat sink
Device-1	175.56	5.7
Device-2	163.33	6.12
Device-3	177.77	5.62
Device-4	187.77	5.33

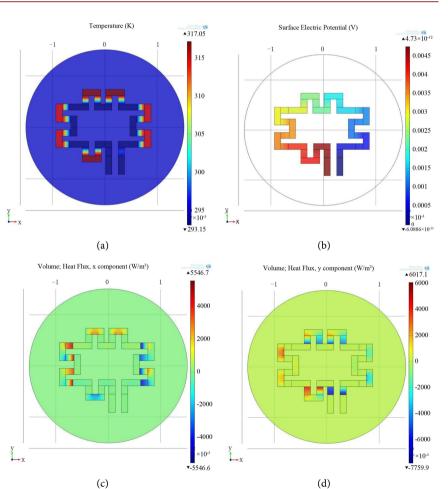


Figure 5. COMSOL simulation of Device-3 with outer junction temperature of 317 K. (a) Temperature distribution; (b) Voltage distribution (c); Heat Flux in the *x*-direction, and (d) Heat Flux in the *y*-direction.

Flux in the *y*-direction. The figure shows that the cold junction temperature is set at 293 K and the hot junction temperature is set at 317 K. From Figure 5(a), it can be seen that there is a temperature gradient across the junctions. This means that there is heat flowing from the hot to the cold junctions, generating electrical potential. The value of the generated potential is shown in Figure 5(b).

As can be seen from Figure 5(b), the voltage potential is the highest at terminal 1 and decreases until it reaches the lowest value at terminal 2. This decrease indicates that the junctions are electrically connected in series. By examining the potential values, we notice that the potential along the copper interconnects is constant. This means that there is little or no voltage drop across the metal. This means also that the emf, generated across terminals 1 and 2, is the summation of the voltage generated by all junctions, with no voltage drop across the series resistance.

To investigate heat dissipation or heat conductivity, the heat flux in the x-direction and the y-direction was simulated. From Figure 5(c), it is clear that there is heat flux across the junctions that are aliened in the x-direction only. Similarly, for the y-component, the flux is only in the junctions that are aliened along the y-direction; Figure 5(d). The Figure shows also that the heat flux in the substrate, between the individual legs, is zero. This indicates that heat exchange takes-place across the junction, and heat sinking is maintained.

5. Analysis

All four devices that are analyzed here have been fabricated in our laboratory, but were tested without a heat sink. It was noticed that after certain voltage, voltage increase did not yield the expected temperature increase. It is believed that the lack of a heat sink allowed both junctions to change their temperature in the direction of thermal equilibrium. The exact phenomenon was also observed in the simulation results. Since the experimental and simulation results are in agreement, it can be claimed that both studies are accurate.

The voltage sensitivity, S_v , and temperature sensitivity are used to characterize the device performance. For experimental results, S_v increased from 93 μ V/K to 132 μ V/K for substrate temperature of 100°C to 400°C. On the other hand, for simulation, S_v increased from 112 μ V/K to 135 μ V/K for substrate temperature of 100°C to 400°C. Although the values of S_v for both cases are close, the increase of S_v with growth temperature is sharper in case of experimental measurements than simulation. This mismatch can be attributed to the fact that simulation was performed assuming that Bi_2T_3 and Sb_2T_3 have constant Seebeck coefficients, regardless of the growth temperature of the materials. In reality, Seebeck coefficient changes with substrate temperature, which is reflected in the experimental measurements, but is not in the simulation analysis.

The simulation results show that sensitivity still increased with substrate temperature, even with using constant Seebeck coefficient. The increase could be due to the increase in the electrical conductivity and the decrease in the thermal conductivity of Bi_2Te_3 with growth temperature [1] [40]. For Sb_2Te_3 , the thermal conductivity is assumed constant and the electrical conductivity was found experimentally to decrease with the growth temperature, but with slower rate [1]. Even with these opposing effects, a moderate increase in the voltage sensitivity with growth temperature was observed.

When a heat sink is utilized, S_v increases with growth temperature, as shown by simulation. S_v increased from 175.56 to 187.77 μ V/K. The increase of S_v for devices with heat sink can be attributed to the absence of a load across terminals 1 and 2. Connecting a load results in drawing current, which, in turn, results in a voltage drop across the device series resistance. This, in turn, reduces the induced voltage across terminals 1 and 2, and consequently, reduces S_v to values closer to those obtained from the experimental measurements. But since, in our simulation, no load was connected at the output, the induced voltage increased, resulting in a higher S_v , as our results indicate.

By studying the sensitivities, one may realize that a device with low voltage sensitivity has high temperature sensitivity and assumes that such a device is most suitable for cooling and heating applications. This may not be true in reality, since device performance, for any application, depends on many factors, including, but not limited to, sensitivity. Hence, device structure, geometry, material properties, and processing should be designed to yield the best results for the intended application.

6. Conclusions

In conclusion, this study shows that reliable testing of thermoelectric devices requires the use of heat sink, to avoid uncontrolled change in the junction temperatures. The study shows also that the output load characteristics affect the device performance. Therefore, for a more accurate analysis of the devices, simulation and experimental measurement should be done with a load connected to the output terminals. The study has also shown that the device should be optimized for the application intended for. For energy harvesting, S_V should be optimized. However, for cooling or heating, S_T should be the parameter to be optimized. These parameters can be optimized by choosing the appropriate material and the optimum design structure that reduces stray elements.

Based on this study, two future works can be proposed: The first is to investigate the influence of device parameters on performance and the stability of the device operation. This will lead to developing design methodology that can be used to achieve the maximum intended performance; The second future work is to investigate the transient response and operation in the time domain. This would be essential for device design, if the device is used as a fast response heat sensor. Small signal analysis requires the development of a small signal equivalent circuit.

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